

Newtonian Mechanics for Undergraduates

Essential Textbooks in Physics

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by *Vijay Tymms*

Essential Textbooks in Physics

Newtonian Mechanics for Undergraduates

Vijay Tymms

Imperial College London, UK

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Contents

1.	Overview	1
1.1	Introduction	1
1.2	Why This Book is Needed	1
1.3	Who Will Benefit From This Book?	2
1.4	Assumed Prior Knowledge	2
1.5	Structure and Topics	3
	Feedback for the Author	4
2.	Introductory Concepts	5
2.1	Quantities, Units, and Coordinate Systems	5
2.1.1	Scalar and Vector Quantities	5
2.1.2	When Vectors Will Be Used and What Knowledge Will Be Assumed	6
2.1.3	Vector Notation in Print and in Handwriting	6
2.1.4	Knowing When a Quantity is Scalar or Vector	7
2.1.5	Units	7
2.1.6	Standard SI Prefixes	8
2.1.7	Coordinate Systems	9
2.2	Time, Displacement, Velocity, and Acceleration . . .	10
2.2.1	Time	10
2.2.2	What is Meant By “Time is Linear and Universal” and Some Musing on Time Travel?	10
2.2.3	Displacement	11

2.2.4	Velocity	12
2.2.5	Acceleration	14
2.3	Force, Mass (and Acceleration)	16
2.3.1	Mass	16
2.3.2	Force	18
2.3.3	Relating Force, Mass, and Acceleration . . .	19
2.3.4	$F = ma$ as a Cause-to-Effect Ratio and Other Examples in Physics	19
2.3.5	Watch out for Careless Alternative Definitions	20
2.3.6	Definitions of the Second, Metre, and Kilogram	20
3.	1D Motion	21
3.1	The Equations for Constant Acceleration	21
3.1.1	Setting up the Basic Situation	21
3.1.2	Finding x as a Function of t	25
3.1.3	Finding v as a Function of x	26
3.1.4	Two More Equations	27
3.1.5	Using the Equations for Constant Acceleration	28
3.2	Time-Dependent Forces	30
3.3	Displacement-Dependent Forces	32
3.4	Velocity-Dependent Forces	35
3.5	More Complicated Forces	36
4.	Newton's First and Second Laws of Motion	37
4.1	Newton's First Law of Motion	37
4.1.1	The Law is Not Valid in Accelerating Reference Frames	37
4.1.2	Nor is the Law Valid on Subatomic Scales . .	38

4.2	Introducing Linear Momentum Before Stating Newton's Second Law	39
4.3	Newton's Second Law of Motion	40
4.4	Derivation of $F = ma$ and the Definition of the Newton	41
4.5	Simple $F = ma$ Examples for a Point Particle	42
4.5.1	No Velocity, Balanced Forces	42
4.5.2	Constant Velocity, Balanced Forces	43
4.5.3	Constant Acceleration, Unbalanced Forces	43
4.5.4	Non-Constant Acceleration, Unbalanced Forces	44
4.5.5	Force Implies Acceleration and Acceleration Implies Force; Deduction and Induction . . .	44
4.6	Alternative Statements of the Laws	45
5.	Types of Force and Free Body Diagrams	47
5.1	Free Body Diagrams	47
5.2	Types of Mechanical Force	48
5.2.1	Weight	48
5.2.2	Normal Contact Force	50
5.2.3	Friction	52
5.2.4	Tension and Compression	57
5.2.5	Upthrust	60
5.2.6	Drag Force	61
5.2.7	Lift	61
6.	Newton's Third Law of Motion	63
6.1	Newton's Third Law of Motion	63
6.2	Newton's Third Law Pairs	64
6.2.1	Type 1: Long Range Forces ("Action at a Distance")	64

6.2.2	Type 2: Contact Forces	66
6.2.3	Type 3: Fluid Pressure Difference Forces . .	71
6.3	Misuses and Apparent Paradoxes	71
6.3.1	Action and Reaction	71
7.	Linear Momentum	73
7.1	Linear Momentum	73
7.2	Change in Momentum: Impulse	73
7.3	The Conservation of Linear Momentum	74
7.3.1	Proof of the Conservation of Momentum for a General Two Particle System	74
7.3.2	Conservation of Momentum for an N -Particle System	75
7.4	Using the Conservation of Linear Momentum	76
7.5	Splitting Momentum Into Components	79
7.5.1	Situations with a Resultant External Force Along One Component	80
7.6	Two Classic Physics Puzzles	80
7.6.1	The Sailing Boat and The Hair Dryer	80
7.6.2	The Lorry Driver and the Geese	82
8.	Work, Energy and Power	85
8.1	Work	85
8.1.1	Definition, Units, and Values	85
8.1.2	More on the Angle between the Force and the Displacement	86
8.1.3	Non-Constant Forces	87
8.1.4	Is the Work Done by Friction Positive or Negative? Some Words on Terrestrial Locomotion	89
8.2	Energy, its Conservation, and Types of Energy . . .	90
8.3	Kinetic Energy and the Work–Energy Theorem . . .	91

8.4	Power	93
8.4.1	Does the Work Done When Lifting an Object Depend on How Fast it is Lifted? . .	94
9.	Potential Energy	95
9.1	Gravitational Potential Energy	95
9.1.1	More Familiar Interpretation	98
9.1.2	Potential Energy is Shared between Two or More Objects	98
9.2	General Case in 1D	98
9.3	Elastic Potential Energy	100
9.3.1	Stored $Energy = \frac{1}{2} \times Constant \times Variable^2$ Formulae Appear Quite a Lot in Physics . .	101
9.4	Conservative and Non-Conservative Forces	102
9.4.1	Introduction	102
9.4.2	Other Properties	103
9.4.3	Lifting a Box	103
9.5	Potential Wells	104
9.6	Mass–Energy Equivalence and $E = mc^2$	106
9.6.1	Mass–Energy in General	106
9.6.2	Stretching a Spring	107
9.6.3	Charging a Battery	108
9.6.4	Kinetic Energy, Dissipation of Heat, and Cups of Tea	108
9.6.5	Climbing a Mountain	109
9.6.6	Combustion, Breathing, and Weight Loss . .	111
9.6.7	Nuclear Reactions	113
10.	Collisions and Rockets	115
10.1	Collisions	115
10.1.1	Elastic Collisions	116
10.1.2	Inelastic Collisions	122

10.1.3	Superelastic Collisions	125
10.2	Reference Frames	126
10.3	Particle–Wall Collisions	128
10.4	Fluid Jet Pressure	129
10.5	Rocket Propulsion	131
10.5.1	The Basic Principle of Rocketry	131
10.5.2	Rocket Propulsion for a Constant Velocity Fuel Ejection	131
11.	Motion on a Curved Path	135
11.1	Uniform Circular Motion	135
11.1.1	General Kinematic Analysis	135
11.1.2	What This Tells Us	137
11.1.3	Example of An Object Travelling Around a Circular Banked Track	138
11.2	Motion on a General Curve with Changing Speed . .	140
11.2.1	More on the General Radius of Curvature and How to Use it with the Circular Motion Equation	140
11.2.2	Example of an Object Sliding Off a Round, Frictionless Hill	142
12.	Simple Harmonic Motion	147
12.1	Amplitude, Period, Frequency and Angular Frequency	147
12.2	Sinusoidal Oscillations	148
12.2.1	A Simple Harmonic Oscillator Does not Necessarily Exhibit SHM	149
12.3	Two Examples of SHM	150
12.3.1	What Does “Small Angle” Mean?	153
12.4	SHM and Uniform Circular Motion	153
12.5	Energy in SHM	153

12.5.1	Kinetic and Potential Energies	153
12.5.2	The Constant, k	155
12.5.3	The Potential Well Approach	155
12.5.4	Example with the Simple Pendulum Revisited	156
12.6	Other Features of SHM	156
13.	Gravitation	157
13.1	Newton's Law of Gravitation	157
13.1.1	The Gravitational Force is Weak	158
13.1.2	Point Masses	159
13.1.3	Example: Circular orbits about a planet (with a preface on Newton's cannon)	159
13.1.4	The Inaccuracy of the Term "Weightless" . .	162
13.2	Gravitational Field Strength	163
13.2.1	Gravitational Field Strength and Weight . .	163
13.2.2	g : Gravitational Field Strength in Nkg^{-1} or Acceleration Due to Gravity in ms^{-2} ?	164
13.2.3	Inertial and Gravitational Mass	164
13.3	Gravitational Potential and Binding Energy	165
13.3.1	Proof of Equation 13.3	166
13.3.2	Escape Velocity	168
13.3.3	Black Holes and the Schwarzschild Radius .	169
13.4	Gravitational Effects of A Spherical Shell	169
13.4.1	The Force on a Mass Outside a Hollow Sphere	170
13.4.2	The Force on a Mass Inside a Hollow Sphere	172
13.5	Planetary Variations in Field Strength	174
14.	Rotational Analogues	177
14.1	Angular Velocity	177

14.2	Angular Acceleration	178
14.3	Rotational Kinetic Energy and Moment of Inertia . .	179
14.3.1	Single Particle	179
14.3.2	Several Particles	179
14.3.3	Continuum of Particles	180
14.3.4	Meaning of Moment of Inertia	181
14.3.5	Common Examples	181
14.4	Torque	184
14.4.1	Rotational Equivalent of Newton's Second Law	185
14.5	Angular Momentum	186
14.6	A Bit More on Scalars, Vectors, and Tensors	186
14.6.1	Angular Velocity vs. Linear Velocity	187
14.6.2	The Moment of Inertia Tensor	188
15.	Equilibrium and Balance	189
15.1	Centre of Mass	189
15.1.1	Discrete Particle System	189
15.1.2	Continuum System	190
15.1.3	L-Shaped Object	191
15.1.4	Importance	191
15.2	Centre of Gravity	192
15.3	Centre of Buoyancy	193
15.4	Equilibrium	194
15.5	Examples of Equilibrium	195
15.5.1	See-Saw	195
15.5.2	Balancing Pencil	195
15.5.3	Leaning Ladder	196
16.	Unbalanced Objects	201
16.1	An Unbalanced Light See-Saw	201
16.2	Rigid Object Toppling About A Pivot	202

16.2.1	The Forces	202
16.2.2	Unstable Equilibrium	203
16.2.3	Stable Equilibrium	203
16.2.4	Toppling	204
16.2.5	Accelerations for a Uniform Rod (with a Note on Why Balancing a Pencil on Your Fingertip is Difficult But Balancing a Broom Handle is Easy)	204
16.2.6	The Tangential Linear Acceleration and a Surprising Result	206
16.2.7	Energy Approach	207
16.2.8	Variation of Forces with Angle	207
16.2.9	Oscillations About the Stable Equilibrium Point	209
17.	Rolling and Sliding	213
17.1	The Condition for Rolling	213
17.1.1	Think About Riding a Bicycle	216
17.2	Rolling Friction — Why Rolling Objects Stop at All	217
17.3	Rolling Down an Inclined Plane	218
17.3.1	Analysis Using Energy	218
17.3.2	Analysis Using Dynamics	220
17.3.3	The Condition for No Slipping	221
17.4	An External Force Causing Rolling on a Flat Surface	222
18.	Angular Momentum	227
18.1	Definition	227
18.2	Torque and Angular Momentum	227
18.3	Moment of Inertia and Angular Momentum	229
18.4	The Conservation of Angular Momentum	229

18.5	Examples of the Conservation of Angular Momentum	230
18.5.1	The Ice Skater (Or Less Agile Person Sat on a Rotating Platform)	230
18.5.2	The Bicycle Wheel Variant	232
18.5.3	Turning Yourself Around Without Translational Motion on An Ice Rink	232
18.5.4	The Physics of the Falling Cat	233
18.5.5	Kepler's Second Law	234
19.	Angular Momentum, Gyroscopes, and Precession	237
19.1	The Gyroscope	237
19.2	Application of Torque about the Pivot to a Spinning Gyro	238
19.3	Precession Formula	241
19.4	Analogy with Linear Circular Motion	242
19.5	Analysis of Precession in Terms of Forces and Velocities	243
19.6	Precession is Nothing to do with the Conservation of Angular Momentum	243
19.7	More Subtle Features of Gyroscopic Motion	245
19.8	The Earth's Precession	245
19.9	Examples and Uses of Gyroscopic Motion	246
	<i>Bibliography</i>	247
	<i>Index</i>	249